# B.Tech (Fourth Semester Computer Science \& Engineering (C.B.C.S)) <br> End Semester Examination Summer - 2023 <br> Course Name: Discrete Mathematics and Graph Theory <br> Course Code: BCS2401 <br> DMT/EFV5734J/3082 <br> [Max.Marks: 60 

Time: 3 Hours]

## Instructions to Candidates:

1. All questions carry marks as indicated.
2. All the sub-questions ( $a, b, c, d$, and e) ofQue. 1 in Section $A$ are compulsory.
3. Solve any two sub-questions in Que. 2 to Que. 6 in Section B.
4. Assume suitable data wherever necessary.
5. Use of non-programmable calculator is permitted.

## Section-A

Que. 1
a) Prove that $\mathrm{A} \cap \mathrm{A}=\mathrm{A}$. 2 (CO1)
b) How many 7 letter words can be formed using the word 'Benzene'. 2 (CO2)
c) Prove that in a distributive lattice if the complement exists then it is unique. 2 (CO3)
d) Find the measure of fuzziness for the fuzzy set $A=\frac{0.2}{x 1}+\frac{0.4}{x 2}$. 2 (CO4)
e) Design the algebraic expression using binary tree. Also draw the venn diagrams. 2 (CO5)
i) $\quad X^{*} Y$
ii) $\quad(a * b) /(c+d)$

## Section - B

Que. 2
a) Find the relation matrix and draw the graph for the relation
$R=\{(1,2),(2,3),(3,4),(2,1)\}$,
Also find the transitive closure of R .
b) Prove that $\mathrm{A} \cap(\mathrm{B}-\mathrm{C})=(\mathrm{A} \cap \mathrm{B})-(\mathrm{A} \cap \mathrm{C})$.
c) Prove by Mathematical induction that the sum of cube of three consecutive integers are divisible by 9 .

## Que. 3

a) Find the minimum number of students in a class to be sure that four out of them are born in the same month.
b) Solve the recurrence relation $a_{n}=a_{n-1}+2, n \geq 2, a_{0}=3$.
c) Find the closed form of generating function for each of following $5(\mathrm{CO} 2)$ Sequences
A) $0,0,1,1,1, \ldots$
B) $1,0,-1,0,1,0,-1,0, \ldots$

Que. 4
a) Prove that fourth roots of unity form a group under multiplication.
b) Show that the lattice $\left(\mathrm{S}_{\mathrm{n}}, \mathrm{D}\right) \mathrm{n}=30$ is a complemented lattice.
c) Show that if $R$ is a ring, for all $a, b \in R$ then
i) $\mathrm{a} \cdot 0=0=0 \cdot \mathrm{a}$
ii) $\quad a \cdot(-b)=(-a) \cdot b=-(a \cdot b)$.
iii) $(-a) \cdot(-b)=a \cdot b$

## Que. 5

a) Find Bounded sum and Bounded Difference for the fuzzy sets $A=\frac{0.2}{x 1}+\frac{0.5}{\mathrm{x} 2}+\frac{0.6}{\mathrm{x} 3}$ and $\mathrm{B}=\frac{0.1}{\mathrm{x} 1}+\frac{0.5}{\mathrm{x} 2}+\frac{0.6}{\mathrm{x} 3}$.
b) Illustrate the matrix and draw the respective graph for following, Let
$\mathrm{A}=\{\mathrm{a} 1, \mathrm{a} 2, \mathrm{a} 3\}$ and $\mathrm{B}=\left\{\mathrm{b}_{1}, \mathrm{~b}_{2}, \mathrm{~b}_{3}, \mathrm{~b}_{4}\right\}$. Let R be the relation from A to B is given by $\frac{0.1}{(a 1, b 3)}+\frac{0.8}{(a 1, b 4)}+\frac{0.8}{(a 2, b 2)}+\frac{0.1}{(a 3, b 1)}+\frac{0.8}{(a 3, b 2)}+\frac{1}{(a 3, b 3)}+\frac{0.8}{(a 3, b 4)}$
c) Find fuzzy relation $\mathrm{R}=\mathrm{A} \times \mathrm{B}, \mathrm{S}=\mathrm{B} \times \mathrm{C}$ if fuzzy sets

5 (CO4)

5 (CO4)
$5(\mathrm{CO} 4)$
$\mathrm{A}=\left\{\frac{0.3}{30}+\frac{0.7}{60}+\frac{1}{100}\right\}, \mathrm{B}=\left\{\frac{0.2}{20}+\frac{0.4}{40}+\frac{0.6}{60}\right\}$ and $\mathrm{C}=\left\{\frac{0.3}{50}+\frac{0.6}{100}\right\}$.

Que. 6
a) Design a tree for the relation $\mathrm{R}=\{(1,2),(1,3),(1,4),(2,5),(4,6),(4,7)\}$ on a set $A=\{1,2,3,4,5,6,7\}$. Also give the corresponding binary tree.
b) Find the minimal spanning tree of the following graph using Prim's algorithm

c) Find the node base of the following digraph.


